

Chain Replication metadata management in Machi, an immutable file store

Introducing the “humming consensus” algorithm

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1. Origins

This document was first written during the autumn of 2014 for a Basho-only internal audience. Since its original drafts, Machi has been designated by Basho as a full open source software project. This document has been rewritten in 2015 to address an external audience. For an overview of the design of the larger Machi system, please see [5].

2. Abstract

TODO Fix, after all of the recent changes to this document.

Machi is an immutable file store, now in active development by Basho Japan KK. Machi uses Chain Replication¹ to maintain strong consistency of file updates to all replica servers in a Machi cluster.

This document describes the Machi chain manager, the component responsible for managing Chain Replication metadata state. Management of chain metadata, e.g., “What is the current order of servers in the chain?”, remains an open research problem. The current state of the art for Chain Replication metadata management relies on an external oracle (e.g., based on ZooKeeper) or the Elastic Replication [1] algorithm.

The chain manager uses a new technique, based on a variation of CORFU, called “humming consensus”. Humming consensus does not require active participation by all or even a majority of participants to make decisions. Machi’s chain manager bases its logic on humming consensus to make decisions about how to react to changes in its environment, e.g. server crashes, network partitions, and changes by Machi cluster administrators. Once a decision is made during a virtual time epoch, humming consensus will eventually discover if other participants have made a different decision during that epoch. When a differing decision is discovered, new time epochs are proposed in which a new consensus is reached and disseminated to all available participants.

¹ Chain Replication is a variation of primary/backup replication where the order of updates between the primary server and each of the backup servers is strictly ordered into a single “chain”.

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3. Introduction

3.1 What does “self-management” mean?

For the purposes of this document, chain replication self-management is the ability for the N nodes in an N -length chain replication chain to manage the chain’s metadata without requiring an external party to perform these management tasks. Chain metadata state and state management tasks include:

- Preserving stable knowledge of chain membership (i.e. all nodes in the chain, regardless of operational status). We expect that a systems administrator will make all “permanent” decisions about chain membership.
- Using passive and/or active techniques to track operational state/status, e.g., up, down, restarting, full data sync in progress, partial data sync in progress, etc.
- Choosing the run-time replica ordering/state of the chain, based on current member status and past operational history. All chain state transitions must be done safely and without data loss or corruption.
- When a new node is added to the chain administratively or old node is restarted, adding the node to the chain safely and perform any data synchronization/repair required to bring the node’s data into full synchronization with the other nodes.

3.2 Ultimate goal: Preserve data integrity of Chain Replicated data

Preservation of data integrity is paramount to any chain state management technique for Machi. Loss or corruption of chain data must be avoided.

3.3 Goal: Contribute to Chain Replication metadata management research

We believe that this new self-management algorithm, humming consensus, contributes a novel approach to Chain Replication metadata management. Typical practice in the IT industry appears to favor using an external oracle, e.g., built on top of ZooKeeper as a trusted coordinator.

See Section 4 for a brief review of techniques used today.

3.4 Goal: Support both eventually consistent & strongly consistent modes of operation

Chain Replication was originally designed by van Renesse and Schneider [19] for applications that require strong consistency, e.g. sequential consistency. However, Machi has use cases where more relaxed eventual consistency semantics are sufficient. We wish to use the same Chain Replication management technique for both strong and eventual consistency environments.

3.5 Anti-goal: Minimize churn

Humming consensus's goal is to manage Chain Replication metadata safely. If participants have differing notions of time, e.g., running on extremely fast or extremely slow hardware, then humming consensus may "churn" rapidly in different metadata states in such a way that the chain's data is effectively unavailable.

In practice, however, any series of network partition changes that cause humming consensus to churn will cause other management techniques (such as an external "oracle") similar problems. [Proof by handwaving assertion.] (See also: Section 5.3)

4. Review of current Chain Replication metadata management methods

We briefly survey the state of the art of research and industry practice of chain replication metadata management options.

4.1 "Leveraging Sharding in the Design of Scalable Replication Protocols" by Abu-Libdeh, van Renesse, and Vigfusson

Multiple chains are arranged in a ring (called a "band" in the paper). The responsibility for managing the chain at position N is delegated to chain $N-1$. As long as at least one chain is running, that is sufficient to start/bootstrap the next chain, and so on until all chains are running. This technique is called "Elastic Replication".

The paper then estimates mean-time-to-failure (MTTF) and suggests a "band of bands" topology to handle very large clusters while maintaining an MTTF that is as good or better than other management techniques.

NOTE: If the chain self-management method proposed for Machi does not succeed, this paper's technique is our best fallback recommendation.

4.2 An external management oracle, implemented by ZooKeeper

This is not a recommendation for Machi: we wish to avoid using ZooKeeper and any other "large" external service dependency. See the "Assumptions" section of [5] for Machi's overall design assumptions and limitations.

However, many other open source software products use ZooKeeper for exactly this kind of critical metadata replica management problem.

4.3 An external management oracle, implemented by Riak Ensemble

This is a much more palatable choice than option 4.2 above. We also wish to avoid an external dependency on something as big as Riak Ensemble. However, if it comes between choosing Riak Ensemble or choosing ZooKeeper, the choice feels quite clear: Riak Ensemble will win, unless there is some critical feature missing from Riak Ensemble. If such an unforeseen missing feature is discovered, it would probably be preferable to add the feature to Riak Ensemble rather than to use ZooKeeper (and for Basho to document ZK, package ZK, provide commercial ZK support, etc.).

4.4 An external management oracle, implemented by active/standby application failover

This technique has been used in production of HibariDB. The customer very carefully deployed the oracle using the Erlang/OTP "application controller" on two machines to provide active/standby failover of the management oracle. The customer was willing to monitor this service very closely and was prepared to intervene manually during network partitions. (This controller is very susceptible to "split brain syndrome".) While this feature of Erlang/OTP is useful in other environments, we believe it is not sufficient for Machi's needs.

5. Assumptions

Given a long history of consensus algorithms (viewstamped replication, Paxos, Raft, et al.), why bother with a slightly different set of assumptions and a slightly different protocol?

The answer lies in one of our explicit goals: to have an option of running in an "eventually consistent" manner. We wish to remain available, even if we are partitioned down to a single isolated node. VR, Paxos, and Raft alone are not sufficient to coordinate service availability at such small scale. The humming consensus algorithm can manage both strongly consistency systems (i.e., the typical use for Chain Replication) as well as eventually consistent data systems.

5.1 The CORFU protocol is correct

This work relies tremendously on the correctness of the CORFU protocol [2], a cousin of the Paxos protocol. If the implementation of this self-management protocol breaks an assumption or prerequisite of CORFU, then we expect that Machi's implementation will be flawed.

5.2 Communication model

The communication model is asynchronous point-to-point messaging. The network is unreliable: messages may be arbitrarily dropped and/or reordered. Network partitions may occur at any time. Network partitions may be asymmetric, e.g., a message can be sent successfully from $A \rightarrow B$, but messages from $B \rightarrow A$ can be lost, dropped, and/or arbitrarily delayed.

System participants may be buggy but not actively malicious/Byzantine.

5.3 Time model

Our time model is per-node wall-clock time clocks, loosely synchronized by NTP.

The protocol and algorithm presented here do not specify or require any timestamps, physical or logical. Any mention of time inside of data structures are for human and/or diagnostic purposes only.

Having said that, some notion of physical time is suggested occasionally for purposes of efficiency. For example, some “sleep time” between iterations of the algorithm: there is no need to “busy wait” by executing the algorithm as many times per minute as possible. See also Section 10.2.1.

5.4 Failure detector model

We assume that the failure detector that the algorithm uses is weak, it’s fallible, and it informs the algorithm in boolean status updates/toggles as a node becomes available or not.

5.5 Data consistency: strong unless otherwise noted

Most discussion in this document assumes a desire to preserve strong consistency in all data managed by Machi’s chain replication. We use the short-hand notation “CP mode” to describe this default mode of operation, where “C” and “P” refer to the CAP Theorem [9].

However, there are interesting use cases where Machi is useful in a more relaxed, eventual consistency environment. We may use the short-hand “AP mode” when describing features that preserve only eventual consistency. Discussion of strongly consistent CP mode is always the default; exploration of AP mode features in this document will always be explicitly noted.

5.6 The reader is familiar with CORFU

Machi borrows heavily from the techniques and data structures used by CORFU [, corfu1][? , corfu2] We hope that the reader is familiar with CORFU’s features, including:

- write-once registers for log data storage,
- the epoch, which defines a period of time when a cluster’s configuration is stable,
- strictly increasing epoch numbers, which are identifiers for particular epochs,
- projections, which define the chain order and other details of data replication within the cluster, and
- the wedge state, used by servers to coordinate cluster changes during epoch transitions.

6. The projection store

The Machi chain manager relies heavily on a key-value store of write-once registers called the “projection store”. Each Machi node maintains its own projection store. The store’s

keyspace is divided into two halves (described below), each with different rules for who can write keys to that half of the store.

The store’s key is a 2-tuple of a positive integer and the half of the partition, the “public” half or the “private” half. The integer represents the epoch number of the projection stored with this key. The store’s value is either the special ‘unwritten’ value² or else a binary blob that is immutable thereafter; the projection data structure is serialized and stored in this binary blob. See 7.1 for more detail.

6.1 The publicly-writable half of the projection store

The publicly-writable projection store is used to share information during the first half of humming consensus algorithm. Projections in the public half of the store form a log of suggestions³ by humming consensus participants for how they wish to change the chain’s metadata state.

Any chain member may write to the public half of the store. Any chain member may read from the public half of the store.

6.2 The privately-writable half of the projection store

The privately-writable projection store is used to store the Chain Replication metadata state (as chosen by humming consensus) that is in use now by the local Machi server. Earlier projections remain in the private half to keep a historical record of chain state transitions by the local server.

Only the local server may write values into the private half of store. Any chain member may read from the private half of the store.

The private projection store serves multiple purposes, including:

- Remove/clear the local server from “wedge state”.
- Act as a world-readable indicator of what projection that the local server is currently using. The current projection will be called $P_{current}$ throughout this document.
- Act as the local server’s log/history of its sequence of $P_{current}$ projection changes.

7. Projections: calculation, storage, and use

Machi uses a “projection” to determine how its Chain Replication replicas should operate; see [5] and [2]. The concept of a projection is borrowed from CORFU but has a longer history, e.g., the Hibari key-value store [7] and goes back in research for decades, e.g., Porcupine [18].

The projection defines the operational state of Chain Replication’s chain order as well the (re-)synchronization of data managed by by newly-added/failed-and-now-recovering

² We use \perp to denote the unwritten value.

³ I hesitate to use the words “propose” or “proposal” anywhere in this document . . . until I’ve done a more formal analysis of the protocol. Those words have too many connotations in the context of consensus protocols such as Paxos and Raft.

```

-type m_server_info() :: {Hostname, Port,...}.
-record(projection, {
    epoch_number      :: m_epoch_n(),
    epoch_csum       :: m_csum(),
    creation_time     :: now(),
    author_server     :: m_server(),
    all_members       :: [m_server()],
    active_upi        :: [m_server()],
    repairing         :: [m_server()],
    down_members      :: [m_server()],
    witness_servers   :: [m_server()],
    dbg_annotations   :: proplist()
}).

```

Figure 1. Sketch of the projection data structure

members of the chain. At runtime, a cluster must be able to respond both to administrative changes (e.g., substituting a failed server with replacement hardware) as well as local network conditions (e.g., is there a network partition?).

7.1 The projection data structure

NOTE: This section is a duplicate of the “The Projection and the Projection Epoch Number” section of the “Machi: an immutable file store” design doc [5].

The projection data structure defines the current administration & operational/runtime configuration of a Machi cluster’s single Chain Replication chain. Each projection is identified by a strictly increasing counter called the epoch projection number (or more simply “the epoch”).

Projections are calculated by each server using input from local measurement data, calculations by the server’s chain manager (see below), and input from the administration API. Each time that the configuration changes (automatically or by administrator’s request), a new epoch number is assigned to the entire configuration data structure and is distributed to all servers via the server’s administration API.

Pseudo-code for the projection’s definition is shown in Figure 1. To summarize the major components:

- `epoch_number` and `epoch_csum` The epoch number and projection checksum together form the unique identifier for this projection.
- `creation_time` Wall-clock time, useful for humans and general debugging effort.
- `author_server` Name of the server that calculated the projection.
- `all_members` All servers in the chain, regardless of current operation status.
- `active_upi` All active chain members that we know are fully repaired/in-sync with each other and therefore the Update Propagation Invariant (Section A.1) is always true.

- `repairing` All running chain members that are in active data repair procedures.
- `down_members` All members that the `author_server` believes are currently down or partitioned.
- `witness_servers` If witness servers (Section ??) are used in strong consistency mode, then they are listed here. The set of `witness_servers` is a subset of `all_members`.
- `dbg_annotations` A “kitchen sink” property list, for code to add any hints for why the projection change was made, delay/retry information, etc.

7.2 Why the checksum field?

According to the CORFU research papers, if a server node S or client node C believes that epoch E is the latest epoch, then any information that S or C receives from any source that an epoch $E + \delta$ (where $\delta > 0$) exists will push S into the “wedge” state and force C into a mode of searching for the projection definition for the newest epoch.

In the humming consensus description in Section 10, it should become clear that it’s possible to have a situation where two nodes make proposals for a single epoch number. In the simplest case, assume a chain of nodes a and b . Assume that a symmetric network partition between a and b happens. Also, let’s assume that operating in AP/eventually consistent mode.

On a ’s network-partitioned island, a can choose an active chain definition of $[A]$. Similarly b can choose a definition of $[B]$. Both a and b might choose the epoch for their proposal to be #42. Because each are separated by network partition, neither can realize the conflict.

When the network partition heals, it can become obvious to both servers that there are conflicting values for epoch #42. If we use CORFU’s protocol design, which identifies the epoch identifier as an integer only, then the integer 42 alone is not sufficient to discern the differences between the two projections.

Humming consensus requires that any projection be identified by both the epoch number and the projection checksum, as described in Section 7.1.

8. Managing projection store replicas

An independent replica management technique very similar to the style used by both Riak Core [12] and Dynamo is used to manage replicas of Machi’s projection data structures. The major difference is that humming consensus *does not necessarily require* successful return status from a minimum number of participants (e.g., a majority quorum).

8.1 Writing to public projection stores

Writing replicas of a projection P_{new} to the cluster’s public projection stores is similar to writing in a Dynamo-like system. The significant difference with Chain Replication is how we interpret the return status of each write operation.

In cases of `error_written` status, the process may be aborted and read repair triggered. The most common reason for `error_written` status is that another actor in the system has concurrently already calculated another (perhaps different⁴) projection using the same projection epoch number.

8.2 Writing to private projection stores

Only the local server/owner may write to the private half of a projection store. Private projection store values are never subject to read repair.

8.3 Reading from public projection stores

A read is simple: for an epoch E , send a public projection read API operation to all participants. Usually, the “get latest epoch” variety is used.

The minimum number of non-error responses is only one.⁵ If all available servers return a single, unanimous value V_u , $V_u \neq \perp$, then V_u is the final result for epoch E . Any non-unanimous values are considered unresolvable for the epoch. This disagreement is resolved by newer writes to the public projection stores during subsequent iterations of humming consensus.

Unavailable servers may not necessarily interfere with making a decision. Humming consensus only uses as many public projections as are available at the present moment of time. Assume that some server S is unavailable at time t and becomes available at some later $t + \delta$. If at $t + \delta$ we discover that S 's public projection store for key E contains some disagreeing value V_{weird} , then the disagreement will be resolved in the exact same manner that would have been used as if we had seen the disagreeing values at the earlier time t .

8.4 Read repair: repair only unwritten values

The “read repair” concept is also shared with Riak Core and Dynamo systems. However, Machi has situations where read repair cannot truly “fix” a key because two different values have been written by two different replicas. Machi's projection store is write-once, and there is no “undo” or “delete” or “overwrite” in the projection store API.⁶ Machi's projection store read repair can only repair values that are unwritten, i.e., currently storing \perp .

The value used to repair unwritten \perp values is the “best” projection that is currently available for the current epoch E . If there is a single, unanimous value V_u for the projection at epoch E , then V_u is used to repair all projections stores at

⁴The `error_written` may also indicate that another server has performed read repair on the exact projection P_{new} that the local server is trying to write!

⁵The local projection store should always be available, even if no other remote replica projection stores are available.

⁶It doesn't matter what caused the two different values. In case of multiple values, all participants in humming consensus merely agree that there were multiple suggestions at that epoch which must be resolved by the creation and writing of newer projections with later epoch numbers.

E that contain \perp values. If the value of K is not unanimous, then the “highest ranked value” V_{best} is used for the repair; see Section 10.5 for a description of projection ranking.

If a non- \perp value exists, then by definition⁷ this value is immutable. The only conflict resolution path is to write a new projection with a newer and larger epoch number. Once a public projection with epoch number E is written, projections with epochs smaller than E are ignored by humming consensus.

9. Phases of projection change, a prelude to Humming Consensus

Machi's projection changes use four discrete phases: network monitoring, projection calculation, projection storage, and adoption of new projections. The phases are described in the subsections below. The reader should then be able to recognize each of these phases when reading the humming consensus algorithm description in Section 10.

9.1 Network monitoring

Monitoring of local network conditions can be implemented in many ways. None are mandatory, as far as this RFC is concerned. Easy-to-maintain code should be the primary driver for any implementation. Early versions of Machi may use some/all of the following techniques:

- Other FLU file and projection store API requests.
- Internal “no op” FLU-level protocol request & response.
- Network tests via ICMP ECHO_REQUEST, a.k.a. ping(8)

Output of the monitor should declare the up/down (or alive/unknown) status of each server in the projection. Such Boolean status does not eliminate fuzzy logic, probabilistic methods, or other techniques for determining availability status. A hard choice of boolean up/down status is required only by the projection calculation phase (Section 9.2).

9.2 Calculating a new projection data structure

A new projection may be required whenever an administrative change is requested or in response to network conditions (e.g., network partitions, crashed server).

Projection calculation is a pure computation, based on input of:

1. The current projection epoch's data structure
2. Administrative request (if any)
3. Status of each server, as determined by network monitoring (Section 9.1).

Decisions about *when* to calculate a projection are made using additional runtime information. Administrative change requests probably should happen immediately. Change based on network status changes may require retry logic and delay/sleep time intervals.

⁷Definition of a write-once register

9.3 Writing a new projection

In Machi’s case, the writing a new projection phase is very straightforward; see Section 8.1 for the technique for writing projections to all participating servers’ projection stores. Humming Consensus does not care if the writes succeed or not. The next phase, adopting a new projection, will determine which write operations are usable.

9.4 Adoption a new projection

It may be helpful to consider the projections written to the cluster’s public projection stores as “suggestions” for what the cluster’s new projection ought to be. (We avoid using the word “proposal” here, to avoid direct parallels with protocols such as Raft and Paxos.)

In general, a projection P_{new} at epoch E_{new} is adopted by a server only if the change in state from the local server’s current projection to new projection, $P_{current} \rightarrow P_{new}$, will not cause data loss: the Update Propagation Invariant and all other safety checks required by chain repair in Section 12 are correct. For example, any new epoch must be strictly larger than the current epoch, i.e., $E_{new} > E_{current}$.

Machi first reads the latest projection from all available public projection stores. If the result is not a single unanimous projection, then we return to the step in Section 9.2. If the result is a *unanimous* projection P_{new} in epoch E_{new} , and if P_{new} does not violate chain safety checks, then the local node will:

- write $P_{current}$ to the local private projection store, and
- set its local operating state $P_{current} \leftarrow P_{new}$.

10. Humming Consensus

Humming consensus describes consensus that is derived only from data that is visible/available at the current time. It’s OK if a network partition is in effect and not all chain members are available; the algorithm will calculate a rough consensus despite not having input from all chain members.

- When operating in eventual consistency mode, humming consensus may reconfigure a chain of length N into N independent chains of length 1. When a network partition heals, the humming consensus is sufficient to manage the chain so that each replica’s data can be repaired/merged/reconciled safely. Other features of the Machi system are designed to assist such repair safely.
- When operating in strong consistency mode, any chain shorter than the quorum majority of all members is invalid and therefore cannot be used. Any server with a too-short chain cannot not move itself out of wedged state and is therefore unavailable for general file service. In very general terms, this requirement for a quorum majority of surviving participants is also a requirement for Paxos, Raft, and ZAB. See Section 11 for a proposal to handle “split brain” scenarios while in CP mode.

If a projection suggestion is made during epoch E , humming consensus will eventually discover if other participants have made a different suggestion during epoch E . When a conflicting suggestion is discovered, newer & later time epochs are defined to try to resolve the conflict.

The next portion of this section follows the same pattern as Section 9: network monitoring, calculating new projections, writing projections, then perhaps adopting the newest projection (which may or may not be the projection that we just wrote).

This section will refer heavily to Figure 2, a flowchart of the humming consensus algorithm. The following notation is used by the flowchart and throughout this section.

- Author** The name of the server that created the projection.
- Rank** Assigns a numeric score to a projection, see Section 10.5.
- E** The epoch number of a projection.
- UPI** “Update Propagation Invariant”. The UPI part of the projection is the ordered list of chain members where the Update Propagation Invariant of the original Chain Replication paper [19] is preserved. All UPI members of the chain have their data fully synchronized and consistent, except for updates in-process at the current instant in time. The UPI list is what Chain Replication usually considers “the chain”. For strongly consistent read operations, all clients send their read operations to the tail/last member of the UPI server list. In Hibari’s implementation of Chain Replication [7], the chain members between the “head” and “official tail” (inclusive) are what Machi calls the UPI server list. (See also Section A.1.)
- Repairing** The ordered list of nodes that are in repair mode, i.e., synchronizing their data with the UPI members of the chain. In Hibari’s implementation of Chain Replication, any chain members that follow the “official tail” are what Machi calls the repairing server list.
- Down** The list of chain members believed to be down, from the perspective of the author.
- $P_{current}$** The projection actively used by the local node right now. It is also the projection with largest epoch number in the local node’s *private* projection store.
- $P_{newprop}$** A new projection suggestion, as calculated by the local server (Section 10.2).
- P_{latest}** The highest-ranked projection with the largest single epoch number that has been read from all available *public* projection stores.
- Unanimous** The P_{latest} projection is unanimous if all replicas in all accessible public projection stores are effectively identical. All major elements such as the epoch number, checksum, and UPI list must be the same.

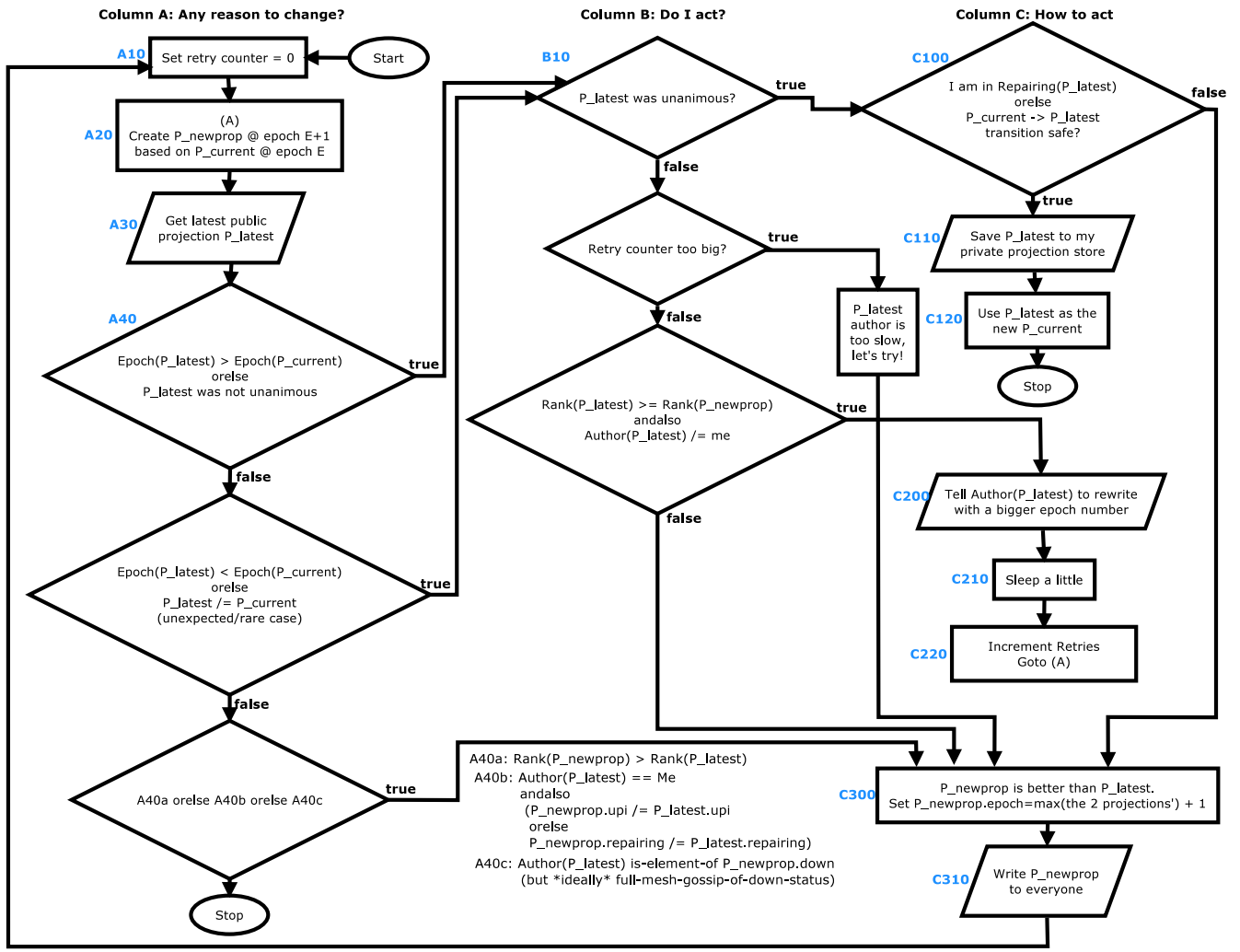


Figure 2. Humming consensus flow chart

$P_{current} \rightarrow P_{latest}$ **transition safe?** A predicate function to check the sanity & safety of the transition from the local server's $P_{current}$ to the P_{latest} projection.

Stop state One iteration of the self-management algorithm has finished on the local server.

The flowchart has three columns, from left to right:

Column A Is there any reason to act?

Column B Do I act?

Column C How do I act?

C1xx Save latest suggested projection to local private store, unwedge, then stop.

C2xx Ask the author of P_{latest} to try again, then we wait, then iterate.

C3xx Our new projection $P_{newprop}$ appears best, so write it to all public projection stores, then iterate.

The Erlang source code that implements the Machi chain manager is structured as a state machine where the function executing for the flowchart's state is named by the approximate location of the state within the flowchart. Most flowchart states in a column are numbered in increasing order, top-to-bottom. These numbers appear in blue in Figure 2. Some state numbers, such as A40, describe multiple flowchart states; the Erlang code for that function, e.g. `react_to_env_A40()`, implements the logic for all such flowchart states.

10.1 Network monitoring

The actions described in this section are executed in the top part of Column A of Figure 2. See also, Section 9.1.

In today's implementation, there is only a single criterion for determining the alive/perhaps-not-alive status of a remote server S : is S 's projection store available now? This question is answered by attempting to read the projection store on server S . If successful, then we assume that S and

all of S 's network services are available. If S 's projection store is not available for any reason (including timeout), we inform the local "fitness server" that we have had a problem querying S . The fitness service may then take additional monitoring/querying actions before informing us (in a later iteration) that S should be considered down.

10.2 Calculating a new projection data structure

The actions described in this section are executed in the top part of Column A of Figure 2. See also, Section 9.2.

Execution starts at "Start" state of Column A of Figure 2. Rule $A20$'s uses judgement from the local "fitness server" to select a definite boolean up/down status for each participating server.

10.2.1 When to calculate a new projection

The Chain Manager schedules a periodic timer to act as a reminder to calculate a new projection. The timer interval is typically 0.5–2.0 seconds, if the cluster has been stable. A client may call an external API call to trigger a new projection, e.g., if that client knows that an environment change has happened and wishes to trigger a response prior to the next timer firing (e.g. at state $C200$).

It's recommended that the timer interval be staggered according to the participant ranking rules in Section 10.5; higher-ranked servers use shorter timer intervals. Staggering sleep timers is not required, but the total amount of churn (as measured by suggested projections that are ignored or immediately replaced by a new and nearly-identical projection) is lower when using staggered timers.

10.3 Writing a new projection

See also: Section 9.3.

To focus very specifically about writing a projection, Figure 2 shows that writing a private projection is done by state $C110$ and that writing a public projection is done by states $C300$ and $C310$.

Broadly speaking, there are a number of decisions made in all three columns of Figure 2 to decide if and when a projection should be written at all. Sometimes, the best action is to do nothing.

10.3.1 Column A: Is there any reason to change?

The main tasks of the flowchart states in Column A is to calculate a new projection P_{new} . Then we try to figure out which projection has the greatest merit: our current projection $P_{current}$, the new projection P_{new} , or the latest epoch P_{latest} . If our local $P_{current}$ projection is best, then there's nothing more to do.

10.3.2 Column B: Do I act?

The main decisions that states in Column B need to make are:

- Is the P_{latest} projection written unanimously (as far as we call tell right now)? If yes, then we consider using it for our new internal state; go to state $C100$.
- We compare P_{latest} projection to our local P_{new} . If P_{latest} is better, then we wait for a while. The waiting loop is broken by a local retry counter. If the counter is small enough, we wait (via state $C200$). While we wait, the author of the P_{latest} projection will have an opportunity to re-write it in a newer epoch unanimously. If the retry counter is too big, then we break out of our loop and go to state $C300$.
- Otherwise we go to state $C300$, where we try to write our P_{new} to all public projection stores because, as far as we can discern, our projection is best and everyone else ought to know it.

It's notable that if P_{new} is truly the best projection available at the moment, it must always first be written to everyone's public projection stores and only afterward processed through another monitor & calculate loop through the flowchart.

10.3.3 Column C: How do I act?

This column contains three variations of how to act:

C1xx Try to adopt the P_{latest} suggestion. If the transition between $P_{current}$ to P_{latest} isn't safe, then jump to $C300$. If it is completely safe, we'll use it by storing P_{latest} in our local private projection store and then adopt it by setting $P_{current} = P_{latest}$.

C2xx Do nothing but sleep a while. Then we loop back to state $A20$ and step through the flowchart loop again. Optionally, we might want to poke the author of P_{latest} to ask it to write its proposal unanimously in a later epoch.

C3xx We try to replicate our P_{new} suggestion to all local projection stores, because it seems best.

10.4 Adopting a new projection

See also: Section 9.4.

The latest projection P_{latest} is adopted by a Machi server at epoch E if the following two requirements are met:

#1: All available copies of P_{latest} are unanimous/identical
If we read two projections at epoch E , P_E^1 and P_E^2 , with different checksum values, then we must consider $P_E^2 \neq P_E^1$ and therefore the suggested projections at epoch E are not unanimous.

#2: The transition from current \rightarrow new projection is safe
Given the current projection $P_{current}$, the projection P_{latest} is evaluated by numerous rules and invariants, relative to $P_{current}$. If such rule or invariant is violated/false, then the local server will discard P_{latest} .

The transition from $P_{current} \rightarrow P_{latest}$ is protected by rules and invariants that include:

1. The Erlang data types of all record members are correct.
2. The members of the UPI, repairing, and down lists contain no duplicates and are in fact mutually disjoint.
3. The author node is not down (as far as we can observe).
4. There is no re-ordering of the UPI list members: the relative order of the UPI list members in both projections must be strictly maintained. The same re-ordering restriction applies to all servers in P_{latest} 's repairing list relative to $P_{current}$'s repairing list.
5. Any server S that is newly-added to P_{latest} 's UPI list must appear in the tail the UPI list. Furthermore, S must have been in $P_{current}$'s repairing list and had successfully completed file repair prior to S 's promotion from the repairing list to the tail of the UPI list.

10.5 Ranking projections

A projection's rank is based on the epoch number (higher always wins), chain length (larger wins), number & state of any repairing members of the chain (larger wins), and node name of the author server (as a tie-breaking criteria).

11. "Split brain" management in CP Mode

Split brain management is a thorny problem. The method presented here is one based on pragmatics. If it doesn't work, there isn't a serious worry, because Machi's first serious use case all require only AP Mode. If we end up falling back to "use Riak Ensemble" or "use ZooKeeper", then perhaps that's fine enough. Meanwhile, let's explore how a completely self-contained, no-external-dependencies CP Mode Machi might work.

Wikipedia's description of the quorum consensus solution⁸ is nice and short:

A typical approach, as described by Coulouris et al.,[4] is to use a quorum-consensus approach. This allows the sub-partition with a majority of the votes to remain available, while the remaining sub-partitions should fall down to an auto-fencing mode.⁹

This is the same basic technique that both Riak Ensemble and ZooKeeper use. Machi's extensive use of write-once registers are a big advantage when implementing this technique. Also very useful is the Machi "wedge" mechanism, which can automatically implement the "auto-fencing" that the technique requires. All Machi servers that can communicate with only a minority of other servers will automatically "wedge" themselves, refuse to author new projections, and refuse all file API requests until communication with the majority can be re-established.

⁸ See [http://en.wikipedia.org/wiki/Split-brain_\(computing\)](http://en.wikipedia.org/wiki/Split-brain_(computing)).

⁹ Any server on the minority side refuses to operate because it is, so to speak, "on the wrong side of the fence."

Partition "side" Quorum UPI	Partition "side" Minority UPI
$[S_1, S_0, S_2]$	\emptyset
$[W_0, S_1, S_0]$	$[W_1, S_2]$
$[W_1, W_0, S_1]$	$[S_0, S_2]$

Figure 3. Illustration of witness servers: on the left side, witnesses provide enough servers to form a UPI chain of quorum length. Servers on the right side cannot suggest a quorum UPI chain and therefore wedge themselves. Under real conditions, there may be multiple minority "sides".

11.1 The quorum: witness servers vs. real servers

In any quorum-consensus system, at least $2f + 1$ participants are required to survive f participant failures. Machi can borrow an old technique of "witness servers" to permit operation despite having only a minority of "real" servers.

A "witness server" is one that participates in the network protocol but does not store or manage all of the state that a "real server" does. A "real server" is a Machi server as described by this RFC document. A "witness server" is a server that only participates in the projection store and projection epoch transition protocol and a small subset of the file access API. A witness server doesn't actually store any Machi files. A witness server's state is very tiny when compared to a real Machi server.

A mixed cluster of witness and real servers must still contain at least a quorum $f + 1$ participants. However, as few as one of them may be a real server, and the remaining f are witness servers. In such a cluster, any majority quorum must have at least one real server participant.

Witness servers are always placed at the front of the chain.

When in CP mode, any server that is on the minority side of a network partition and thus cannot calculate a new projection that includes a quorum of servers will enter wedge state and remain wedged until the network partition heals enough to communicate with a quorum of FLUs. This is a nice property: we automatically get "fencing" behavior.

11.2 Witness server data and protocol changes

Some small changes to the projection's data structure are required (relative to the initial spec described in [5]). The projection itself needs new annotation to indicate the operating mode, AP mode or CP mode. The state type notifies the chain manager how to react in network partitions and how to calculate new, safe projection transitions and which file repair mode to use (Section 12). Also, we need to label member server servers as real- or witness-type servers.

Write API requests are processed by witness servers in *almost but not quite* no-op fashion. The only requirement of a witness server is to return correct interpretations of local projection epoch numbers, via the `error_bad_epoch` and `error_wedged` error codes. In fact, a new API call

is sufficient for querying witness servers: $\{\text{check_epoch}, \text{m_epoch}()\}$. Any client write operation sends the `check_epoch` API command to witness servers and sends the usual `write_req` command to real servers.

11.3 Restarting after entire chain crashes

There’s a corner case that requires additional safety checks to preserve strong consistency: restarting after the entire chain crashes.

The default restart behavior for the chain manager is to start the local server S with $P_{\text{current}} = P_{\text{zero}}$, i.e., S believes that the current chain length is zero. Then S ’s chain manager will attempt to join the chain by waiting for another active chain member S' to notice that S is now available. Then S' ’s chain manager will automatically suggest a projection where S is added to the repairing list. If there is no other active server, then S will suggest projection P_{one} , a chain of length one where S is the sole UPI member of the chain.

The default restart strategy cannot work correctly if: a) all members of the chain crash simultaneously (e.g., power failure), or b) the UPI chain was not at maximum length (i.e., no chain members are under repair or down). For example, assume that the cluster consists of servers S_a , S_b , and witness W_0 . Assume that the UPI chain is $P_{\text{one}} = [W_0, S_a]$ when a power failure halts the entire data center. When power is restored, let’s assume server S_b restarts first. S_b ’s chain manager must suggest neither $[S_b]$ nor $[W_0, S_b]$. Clients must not access S_b at this time because we do not know how much stale data S_b may have.

The chain’s operational history is preserved and distributed amongst the participants’ private projection stores. The maximum of the private projection store’s epoch number from a quorum of servers (including witnesses) gives sufficient information to know how to safely restart a chain. In the example above, we must endure the worst-case and wait until S_a also returns to service.

12. File Repair/Synchronization

There are some situations where read-repair of individual byte ranges of files is insufficient and repair of entire files is necessary.

- To synchronize data on servers added to the end of a chain in a projection change. This case covers both adding a new, data-less server and re-adding a previous, data-full server back to the chain.
- To avoid data loss when changing the order of the chain’s existing servers.

Both situations can cause data loss if handled incorrectly. If a violation of the Update Propagation Invariant (see end of Section A) is permitted, then the strong consistency guarantee of Chain Replication can be violated. Machi uses write-once registers, so the number of possible strong consistency

1. Projection P_E says that chain membership is $[S_a]$.
2. A write of bytes B to file F at offset O is successful.
3. An administration API request triggers projection P_{E+1} that expands chain membership is $[S_a, S_b]$. A file repair/resynchronization process is scheduled to start some-time later.
4. FLU S_a crashes.
5. The chain manager on S_b notices S_a ’s crash, decides to create a new projection P_{E+2} where chain membership is $[S_b]$; S_b executes a couple rounds of Humming Consensus, adopts P_{E+2} , unwedges itself, and continues operation.
6. The bytes in B are definitely unavailable at the moment. If server S_a is never re-added to the chain, then B are lost forever.

Figure 4. An illustration of data loss due to careless handling of file repair/synchronization.

violations is smaller than Chain Replication of mutable registers. However, even when using write-once registers, any client that witnesses a written \rightarrow unwritten transition is a violation of strong consistency. Avoiding even this single bad scenario can be a bit tricky; see Figure 4 for a simple example.

12.1 Just “rsync” it!

A simple repair method might loosely be described as “just rsync all files to all servers in an infinite loop.”¹⁰ Unfortunately, such an informal method cannot tell you exactly when you are in danger of data loss and when data loss has actually happened. However, if we always maintain the Update Propagation Invariant, then we know exactly when data loss is imminent or has happened.

We intend to use Machi for multiple use cases, in both require strong consistency and eventual consistency environments. For a use case that implements a CORFU-like service, strong consistency is a non-negotiable requirement. Therefore, we will use the Update Propagation Invariant as the foundation for Machi’s data loss prevention techniques.

12.2 Whole file repair as servers are (re-)added to a chain

Machi’s repair process must preserve the Update Propagation Invariant. To avoid data races with data copying from “U.P. Invariant-preserving” servers (i.e. fully repaired with respect to the Update Propagation Invariant) to servers of unreliable/unknown state, a projection like the one shown in Figure 5 is used. In addition, the operations rules for data

¹⁰The file format suggested in [5] does not actually permit `rsync` as is to be sufficient. A variation of `rsync` would need to be aware of the data/metadata split within each file and only replicate the data section ... and the metadata would still need to be managed outside of `rsync`.

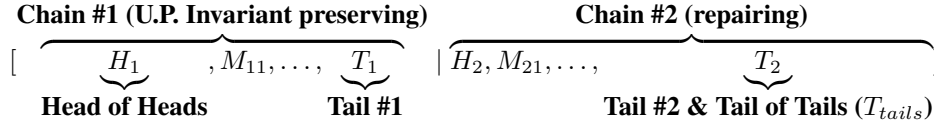


Figure 5. A general representation of a “chain of chains”: a chain prefix of Update Propagation Invariant preserving FLUs (“Chain #1”) with FLUs under repair (“Chain #2”).

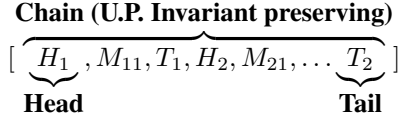


Figure 6. Representation of Figure 5 after all repairs have finished successfully and a new projection has been calculated.

writes and reads must be observed in a projection of this type.

- The system maintains the distinction between “U.P. Invariant-preserving” and “repairing” FLUs at all times. This allows the system to track exactly which servers are known to preserve the Update Propagation Invariant and which servers do not.
- All “repairing” FLUs must be added only at the end of the chain-of-chains.
- All write operations must flow successfully through the chain-of-chains in order, i.e., from “head of heads” to the “tail of tails”. This rule also includes any repair operations.
- All read operations that require strong consistency are directed to Tail #1, as usual.

While normal operations are performed by the cluster, a file synchronization process is initiated to repair any data missing in the tail servers. The sequence of steps differs depending on the AP or CP mode of the system.

12.2.1 Repair in CP mode

In cases where the cluster is operating in CP Mode, CORFU’s repair method of “just copy it all” (from source FLU to repairing FLU) is correct, *except* for the small problem pointed out in Appendix B. The problem for Machi is one of time & space. Machi wishes to avoid transferring data that is already correct on the repairing nodes. If a Machi node is storing 170 TBytes of data, we really do not wish to use 170 TBytes of bandwidth to repair only 2 MBytes of truly-out-of-sync data.

However, it is *vitaly important* that all repairing FLU data be clobbered/overwritten with exactly the same data as the Update Propagation Invariant preserving chain. If this rule is not strictly enforced, then fill operations can corrupt Machi file data. The algorithm proposed is:

1. Change the projection to a “chain of chains” configuration such as depicted in Figure 5.
2. For all files on all FLUs in all chains, extract the lists of written/unwritten byte ranges and their corresponding file data checksums. Send these lists to the tail of tails T_{tails} , which will collate all of the lists into a list of tuples such as $\{\text{FName}, O_{start}, O_{end}, \text{CSum}, \text{FLU_List}\}$ where FLU_List is the list of all FLUs in the entire chain of chains where the bytes at the location $\{\text{FName}, O_{start}, O_{end}\}$ are known to be written (as of the beginning of the current repair period).
3. For chain #1 members, i.e., the leftmost chain relative to Figure 5, repair all file byte ranges for any chain #1 members that are not members of the FLU_List set. This will repair any partial writes to chain #1 that were interrupted, e.g., by a client crash.
4. For all file byte ranges B in all files on all FLUs in all repairing chains where Tail #1’s value is written, send repair data B & metadata to any repairing FLU if the value repairing FLU’s value is unwritten or the checksum is not exactly equal to Tail #1’s checksum.
5. For all file byte ranges B in all files on all FLUs in all repairing chains where Tail #1’s value is unwritten \perp , force B on all repairing FLUs to also be \perp .¹¹

When the repair is known to have copied all missing data successfully, then the chain can change state via a new projection that includes the repaired FLU(s) at the end of the U.P. Invariant preserving chain #1 in the same order in which they appeared in the chain-of-chains during repair. See Figure 6. This transition may progress one server at a time, moving the server formerly in role H_2 to the new role T_1 and adjusting all downstream chain members to “shift left” by one position.

The repair can be coordinated by the T_{tails} FLU or any other FLU or cluster member that has spare capacity to manage the process.

There is no race condition here between the enumeration steps and the repair steps. Why? Because the change in projection at step #1 will force any new data writes to adapt to a new projection. Consider the mutations that either happen before or after a projection change:

¹¹ This may appear to be a violation of write-once register semantics, but in truth, we are fixing the results of partial write failures and therefore must be able to undo any partial write in this circumstance.

- For all mutations M_1 prior to the projection change, the enumeration steps #3 & #4 and #5 will always encounter mutation M_1 . Any repair must write through the entire chain-of-chains and thus will preserve the Update Propagation Invariant when repair is finished.
- For all mutations M_2 starting during or after the projection change has finished, a new mutation M_2 may or may not be included in the enumeration steps #3 & #4 and #5. However, in the new projection, M_2 must be written to all chain of chains members, and such in-order writes will also preserve the Update Propagation Invariant and therefore is also be safe.

12.2.2 Repair in AP Mode

In cases the cluster is operating in AP Mode:

1. In general, follow the steps of the “CP Mode” sequence (above).
2. At step #3, instead of repairing only FLUs in Chain #1, AP mode will repair the byte range of any FLU that is not a member of the `FLU_List` set.
3. Do not use step #5; stop at step #4; under no circumstances go to step #6.

The end result is a big “merge” where any $\{FName, O_{start}, O_{end}\}$ range of bytes that is written on FLU S_w but unwritten from FLU S_u is written down the full chain of chains, skipping any FLUs where the data is known to be written and repairing all such S_u servers. Such writes will also preserve Update Propagation Invariant when repair is finished, even though AP Mode does not require strong consistency that the Update Propagation Invariant provides.

12.3 Whole-file repair when changing server ordering within a chain

This section has been cut — please see Git commit history of this document for discussion.

13. Additional sources for information about humming consensus

- “On Consensus and Humming in the IETF” [11], for background on the use of humming by IETF meeting participants during IETF meetings.
- “On ‘Humming Consensus’, an allegory” [8], for an allegory in homage to the style of Leslie Lamport’s original Paxos paper.

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A. Chain Replication: why is it correct?

See Section 3 of [19] for a proof of the correctness of Chain Replication. A short summary is provide here. Readers interested in good karma should read the entire paper.

A.1 The Update Propagation Invariant

“Update Propagation Invariant” is the original chain replication paper’s name for the $H_i \succeq H_j$ property mentioned in Figure 7. This paper will use the same name. This property may also be referred to by its acronym, “UPI”.

A.2 Chain Replication and strong consistency

The basic rules of Chain Replication and its strong consistency guarantee:

1. All replica servers are arranged in an ordered list C .
2. All mutations of a datum are performed upon each replica of C strictly in the order which they appear in C . A mutation is considered completely successful if the writes by all replicas are successful.
3. The head of the chain makes the determination of the order of all mutations to all members of the chain. If the

head determines that some mutation M_i happened before another mutation M_j , then mutation M_i happens before M_j on all other members of the chain.¹²

4. All read-only operations are performed by the “tail” replica, i.e., the last replica in C .

The basis of the proof lies in a simple logical trick, which is to consider the history of all operations made to any server in the chain as a literal list of unique symbols, one for each mutation.

Each replica of a datum will have a mutation history list. We will call this history list H . For the i^{th} replica in the chain list C , we call H_i the mutation history list for the i^{th} replica.

Before the i^{th} replica in the chain list begins service, its mutation history H_i is empty, $[\]$. After this replica runs in a Chain Replication system for a while, its mutation history list grows to look something like $[M_0, M_1, M_2, \dots, M_{m-1}]$ where m is the total number of mutations of the datum that this server has processed successfully.

Let’s assume for a moment that all mutation operations have stopped. If the order of the chain was constant, and if all mutations are applied to each replica in the chain’s order, then all replicas of a datum will have the exact same mutation history: $H_i = H_j$ for any two replicas i and j in the chain (i.e., $\forall i, j \in C, H_i = H_j$). That’s a lovely property, but it is much more interesting to assume that the service is not stopped. Let’s look next at a running system.

If the entire chain C is processing any number of concurrent mutations, then we can still understand C ’s behavior. Figure 7 shows us two replicas in chain C : replica R_i that’s on the left/earlier side of the replica chain C than some other replica R_j . We know that i ’s position index in the chain is smaller than j ’s position index, so therefore $i < j$. The restrictions of Chain Replication make it true that $\text{length}(H_i) \geq \text{length}(H_j)$ because it’s also that $H_i \supset H_j$, i.e, H_i on the left is always is a superset of H_j on the right.

When considering H_i and H_j as strictly ordered lists, we have $H_i \succeq H_j$, where the right side is always an exact prefix of the left side’s list. This prefixing property is exactly what strong consistency requires. If a value is read from the tail of the chain, then no other chain member can have a prior/older value because their respective mutations histories cannot be shorter than the tail member’s history.

B. Divergence from CORFU’s repair

The original repair design for CORFU is simple and effective, mostly. See Figure 8 for a complete description of the algorithm Figure 9 for an example of a strong consistency violation that can follow.

¹² While necessary for general Chain Replication, Machi does not need this property. Instead, the property is provided by Machi’s sequencer and the write-once register of each byte in each file.

On left side of C		On right side of C
Looking at replica order in chain C :		
i	$<$	j
For example:		
0	$<$	2
It <i>must</i> be true: history lengths per replica:		
$\text{length}(H_i)$	\geq	$\text{length}(H_j)$
For example, a quiescent chain:		
$\text{length}(H_i) = 48$	\geq	$\text{length}(H_j) = 48$
For example, a chain being mutated:		
$\text{length}(H_i) = 55$	\geq	$\text{length}(H_j) = 48$
Example ordered mutation sets:		
$[M_0, M_1, \dots, M_{46}, M_{47}, \dots, M_{53}, M_{54}]$	\supset	$[M_0, M_1, \dots, M_{46}, M_{47}]$
Therefore the right side is always an ordered subset of the left side. Furthermore, the ordered sets on both sides have the exact same order of those elements they have in common.		
The notation used by the Chain Replication paper is shown below:		
$[M_0, M_1, \dots, M_{46}, M_{47}, \dots, M_{53}, M_{54}]$	\succeq	$[M_0, M_1, \dots, M_{46}, M_{47}]$

Figure 7. The “Update Propagation Invariant” as illustrated by Chain Replication protocol history.

1. Destroy all data on the repair destination FLU.
2. Add the repair destination FLU to the tail of the chain in a new projection P_{p+1} .
3. Change the active projection from P_p to P_{p+1} .
4. Let single item read repair fix all of the problems.

Figure 8. Simplest CORFU-style repair algorithm.

1. Write value V to offset O in the log with chain $[S_a]$. This write is considered successful.
2. Change projection to configure chain as $[S_a, S_b]$. All values on FLU S_b are unwritten, \perp . We assume that S_b ’s unwritten values will be written by read-repair operations.
3. FLU server S_a crashes. The new projection defines the chain as $[S_b]$.
4. A client attempts to read offset O and finds \perp . This is a strong consistency violation: the value V should have been found.

Figure 9. An example scenario where the CORFU simplest repair algorithm can lead to a violation of strong consistency.

A variation of the repair algorithm is presented in section 2.5 of a later CORFU paper [3]. However, the re-use a failed server is not discussed there, either: the example of a failed server S_6 uses a new server, S_8 to replace S_6 . Furthermore, the repair process is described as:

“Once S_6 is completely rebuilt on S_8 (by copying entries from S_7), the system moves to projection (C),

where S_8 is now used to service all reads in the range $[40K, 80K]$.”

The phrase “by copying entries” does not give enough detail to avoid the same data race as described in Figure 9. We believe that if “copying entries” means copying only written pages, then CORFU remains vulnerable. If “copying entries” also means “fill any unwritten pages prior to copying them”, then perhaps the vulnerability is eliminated.¹³

¹³ SLF’s note: Probably? This is my gut feeling right now. However, given that I’ve just convinced myself 100% that fill during any possibility of split brain is *not safe* in Machi, I’m not 100% certain anymore than this “easy” fix for CORFU is correct.